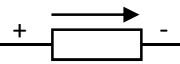


Name: \_\_\_\_\_ Code: \_\_\_\_\_ Group: \_\_\_\_\_

- The symbol “#” is equal to the last digit of your code plus one.
- The grade of each item will be assigned **if and only if** the item is perfect.

1. Given an electrical element: , where  $v(t) = \frac{\#}{10} \frac{di(t)}{dt}$ , and the electric charge in Eq. 1. **a)** Compute the rank of time satisfying  $i(t_?) > \# A$ , **b)** compute  $v(t)$ , **c)** compute and plot the electric power  $p(t)$ , **d)** Find when the power is greater, lower or equal to zero.

2. Given the circuit in Fig. 1, demonstrate the power balance, **a)** before the switch operation, **b)** after the switch operation.

3. Given the circuit in Fig. 2: **a)** Compute the voltage in all nodes if the reference is given by Eq. 2, **b)** If  $v_B = 1.5 * \# * v_C = 2.7 * \# * v_D = 4.1 * \#$ , plot the Electric Potential Diagram, including  $v_{ad}$ , **c)** Compute  $v_{db}$  using at least two different paths, and using stairs-elevator or the Electric Potential Diagram.

$$\text{Eq. 1) } q(t) = \begin{cases} 5 * 10^{-4} C, & t < -1 \text{ ms} \\ 500t^2 (C), & -1 \text{ ms} \leq t < 1 \text{ ms} \\ (\# + 0.5)t - \# * 10^{-3} (C), & 1 \text{ ms} \leq t < 2 \text{ ms} \\ -500t^2 + 3t + (\# - 3)10^{-3} (C), & 2 \text{ ms} \leq t < 3 \text{ ms} \\ (\# + 1.5)10^{-3} (C), & t \geq 3 \text{ ms} \end{cases}$$

$$\text{Eq. 2) } v_{ref} = \begin{cases} a, & \text{if } \# = 1,2,9 \\ b, & \text{if } \# = 3,4,10 \\ c, & \text{if } \# = 5,6 \\ d, & \text{if } \# = 7,8 \end{cases}$$

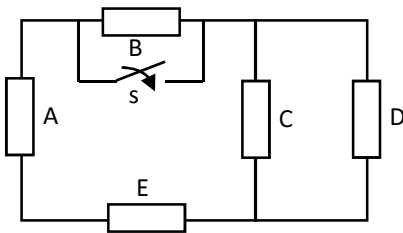


Fig. 1.

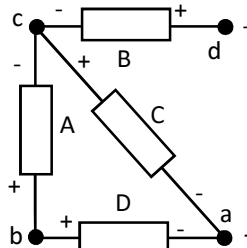


Fig. 2.

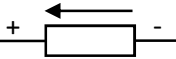
a = 0,6      a = 0,8      a = 0,5  
 b = 0,5      b = 0,8      b = 0,6  
 a = 0,4                      c = 0,6  
 d = 0,2

/1,7      /1,6      /1,7      Great Total:      /5,0

Danilo Rairán, Apr/10/2018

**Note:** # is equal to the last digit of your code plus one.

The points in each item will be assigned **if and only if** the answer and the process are perfect.

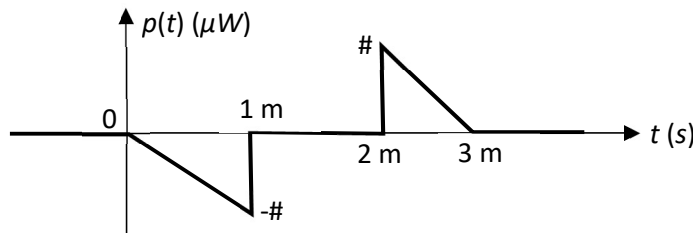
1. Given an electrical element:  answer each question, as follows:

a. Plot  $q(t)$  using Matlab. (0.8 points)

$$q(t) = \begin{cases} 0 \text{ C}, & t < 0 \\ 500t^2 \text{ (C)}, & 0 \leq t < 1 \text{ ms} \\ (\# + 0.5)t - \#10^{-3} \text{ (C)}, & 1 \text{ ms} \leq t < 2 \text{ ms} \\ -500t^2 + 3t + (\# - 3)10^{-3} \text{ (C)}, & 2 \text{ ms} \leq t < 3 \text{ ms} \\ (\# + 1.5)10^{-3} \text{ (C)}, & t \geq 3 \text{ ms} \end{cases}$$

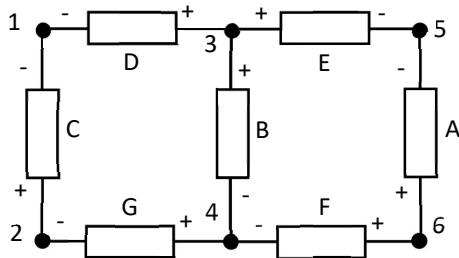
b. Compute  $i(t)$  given  $q(t)$ , by hand (0.5 points)

c. Compute the equation for  $p(t)$  according to the following graph (0.5 points)



d. Compute the voltage  $v(t)$  given the previous data (1.0 points)

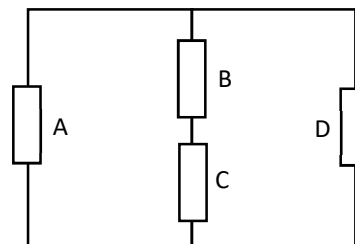
2. Calculate the indicated voltages...



a.  $v_A = \square$ ,  $v_B = ?$ ,  $v_C = \square$ ,  $v_D = \square$ ,  $v_E = \square$ ,  $v_F = \square$ ,  $v_G = \square$  in terms of the voltages in the other elements (0.6 points)

b.  $v_{63} = \square$ ,  $v_{54} = \square$ ,  $v_{32} = \square$ ,  $v_{41} = \square$ ,  $v_{52} = \square$ ,  $v_{61} = \square$ ,  $v_{25} = \square$ ,  $v_{16} = \square$ ,  $v_{45} = \square$ ,  $v_{15} = \square$  in terms of the voltage in the elements (0.6 points)

3. Randomly choose polarity and current sense in the circuit, then demonstrate the power balance. (1 point)



**Introduction to Electricity, Prof. Danilo Rairán, Jun/17/2021, second test**

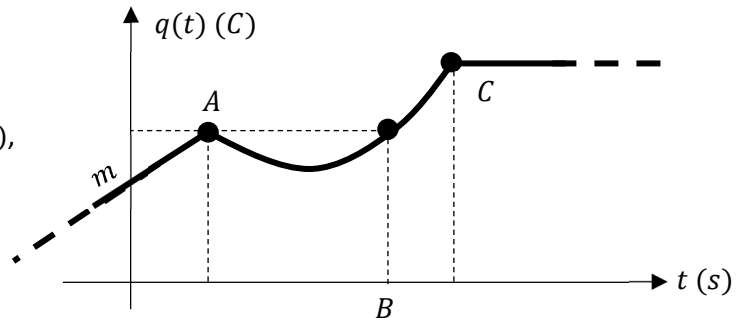
Name: \_\_\_\_\_ Code: \_\_\_\_\_

Group: \_\_\_\_\_ # = a number given by the professor during the test

1. The function  $i(t) = (t - \#)^2 * (t + \#)^2$  (A) is not a parabola but given that the best knowledge we have so far to analyze it is a second order polynomial, then compute a parabola that approximates the function  $i(t)$  as close as possible. Explain the procedure of approximation.

2. If  $m = \# \times 10^{-3}$ ,  $A = (\# \times 10^{-3}, \# \times 10^{-6})$ ,  $B = 2 * \# \times 10^{-3}$ ,  $C = (2.5 * \# \times 10^{-3}, 2 * \# \times 10^{-6})$

- a) compute an equation to describe  $q(t)$ ,
- b) compute  $i(t)$ , c) plot  $i(t)$ .



3. Given the equation for  $i(t)$  answer the following questions: a)  $i(4m) = ?$ , b)  $t = ?$  if  $i = 11 mA$ , c)  $t = ?$  if  $i = 8 mA$ .

$$i(t) = \begin{cases} (-1.5 + \#/7)t - 5m(-1.5 + \#/7) + 10m (A), & t < 5 ms \\ -120t^2 + \frac{12}{5}t + 1m (A), & 5ms < t < 15ms \\ (0.5 + \#/7)t - 15m(0.5 + \#/7) + 10m (A), & t > 15 ms \end{cases}$$

4. It is well known that the price of a house changes as the electric charge in a circuit. That price increased  $(25+\#)$  millions per year, until it reaches  $(500 + 25*\#)$  millions. Changes in the politics to curve that tendency makes that price to be  $(540 + 10*\#)$  millions in three years, and another three years later it is  $(490 + 10*\#)$  millions. Finally, the price continues decreasing linearly until  $(450 + 5*\#)$  millions in two years.

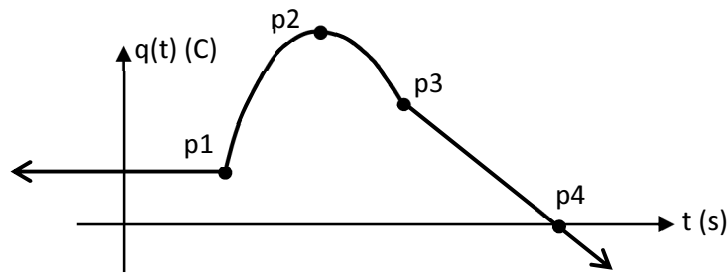
- a) Make a plot describing the price of a house. b) Compute the equation, use scientific notation.

--

- |          |             |             |             |
|----------|-------------|-------------|-------------|
| 1. 1.0/5 | 2. a) 0.7/5 | 3. a) 0.4/5 | 4. a) 0.6/5 |
|          | b) 0.5/5    | b) 0.4/5    | b) 0.9/5    |
|          | c) 0.3/5    | c) 0.2/5    |             |

$x$  = last digit of your code plus one

- Half million cats were devastating the mice population. Nobody knew what was happening until the authorities decided to hire you to make a model. They new that a year ago there were  $x$  billions mice, and just two months ago there were  $x/3$  billions. Everything changes today because the government decided to call a flautist to take all the cats to another country. If you can predict that the mice population will increase to  $x/4$  billions in two months and that they will recover their initial population in six months, a) make a model to describe the mice population from 17/Oct/2018 to 17/Oct/2020; b) could an electric current or electric charge behaves like this mice population? Why?
- If  $p1 = (1.5m, x)$ ,  $p2 = (3.4m, 2.5x)$ ,  $p3 = (5.3m, 2x)$ ,  $p4 = (7.2m, 0)$  in the graph, a) compute  $q(t)$ , b) compute  $i(t)$ , c) plot  $i(t)$ ,



- If  $q(t)$  is given by the following equation, a)  $q(-2.73m) = ?$ , b)  $t_?$  If  $q(t_?) = 0.98m x$ ,

$$q(t) = \begin{cases} 500t^2 + t + (0.5m + 1mx) (C), & t < -1 \text{ ms} \\ -xt (C), & -1 \text{ ms} \leq t < 1 \text{ ms} \\ 500t^2 + t + (-1.5m - 1mx) (C), & t \geq 1 \text{ ms} \end{cases}$$

1 a /15

2 a /8

3 a /5

b /0

b /6

b /12

c /4

**Introduction to Electricity, Prof. Danilo Rairán, Jun/23/2020**

Name: \_\_\_\_\_ Code: \_\_\_\_\_

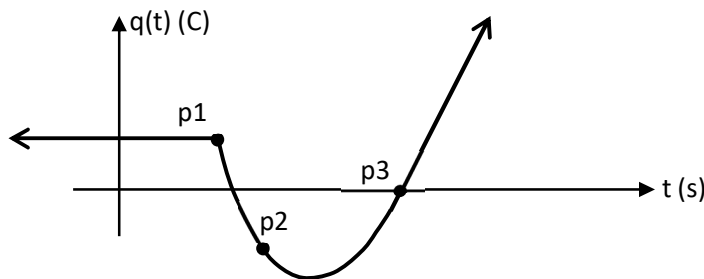
Group: \_\_\_\_\_

# = a number given by the professor during the test

1. Data points in the following table do not describe a parabola, but the best we can do now is to define a parabola that sort of describe them. Compute a parabola that matches the best way possible those points.

t (s)	$2\# \times 10^{-6}$	$3\# \times 10^{-6}$	$4\# \times 10^{-6}$	$5\# \times 10^{-6}$	$6\# \times 10^{-6}$	$7\# \times 10^{-6}$	$8\# \times 10^{-6}$
i (A)	$1 \times 10^{-3}$	$0.809 \times 10^{-3}$	$0.309 \times 10^{-3}$	$-0.309 \times 10^{-3}$	$-0.809 \times 10^{-3}$	$-1 \times 10^{-3}$	$-0.809 \times 10^{-3}$

2. If  $p_1 = (1.5m, \#)$ ,  $p_2 = (3.4m, -1.5\#)$ ,  $p_3 = (6.3m, 0)$  in the graph, **a)** compute  $q(t)$ , **b)** compute  $i(t)$ , **c)** plot  $i(t)$ , knowing that the slope of the line matches the slope of the parabola at  $p_3$ .



3. A monarch butterfly travels crossing countries in a trip that last three generations each round. A biologist estimates that the total amount at the end of the first generation is  $\#10^7$  butterflies. That number is  $1.2 \times \#10^7$  at the end of the second generation, and again  $\#10^7$  at the end of the third generation. However, things were not that good for them after that, they start to decrease 1% every year. If there are baby butterflies every 6 weeks, **a)** make a mathematical model to describe the monarch population including the biologist estimations and another three generations of butterflies after that. **b)** could an electric current or electric charge behave like the monarch population? Why?
4. Given the equation for  $q(t)$  answer following questions. **a)**  $q(4\mu) = ?$  **b)**  $t = ?$  if  $q = 0$  C, **c)**  $t = ?$  if  $\# \times 10^{-3} C < q < 2\# \times 10^{-3} C$ .

$$q(t) = \begin{cases} (10^3 t + 10^{-3})\# (C), t < 1 \mu s \\ \left(\frac{5}{4} 10^3 t + \frac{3}{4} 10^{-3}\right)\# (C), 1 \mu s \leq t < 5 \mu s \\ \left(\frac{-7}{2} 10^3 t + \frac{49}{2} 10^{-3}\right)\# (C), t \geq 5 \mu s \end{cases}$$

- |                             |              |             |
|-----------------------------|--------------|-------------|
| 1) 0.6/5                    | → 15 minutes | 6:29 – 6:44 |
| 2) a) 1/5 b) 0.4/5 c) 0.4/5 | → 35 minutes | 6:52 – 7:27 |
| 3) a) 1.5/5 b) 0/5          | → 40 minutes | 7:33 – 8:13 |
| 4) a) 0.3/5 b) 0.3/5 c) 0.5 | → 20 minutes | 8:20 – 8:40 |

**Segundo parcial, Introducción a la Electricidad, 24 de octubre de 2022, Profesor: Danilo Rairán**

Nombre: \_\_\_\_\_ Código: \_\_\_\_\_ Grupo: \_\_\_\_\_

# = último dígito del código + 1

1. Dados los datos en la tabla, y presentando todo el procedimiento:
  - a. encuentre una línea que aproxime todos los datos, luego haga una aproximación parabólica,
  - b. grafique, tanto los datos de la tabla como las dos aproximaciones en una misma gráfica.

t (s)	-2m	-1m	0	1m	2m	3m	4m	5m
q(t) (C)	-5#	0	1#	4#	15#	40#	85#	156#

2. Dada la ecuación para  $i(t)$ , presente todo el procedimiento para calcular:
  - a.  $t = ?$  si  $i = 12 \text{ mA}$ ,
  - b.  $t = ?$  si  $i = 5 \text{ mA}$ .

$$i(t) = \begin{cases} (-1.5 + \#/7)t - 5m(-1.5 + \#/7) + 10m (A), & t < 5 \text{ ms} \\ -120t^2 + \frac{12}{5}t + 1m (A), & 5ms < t < 15ms \\ (0.5 + \#/7)t - 15m(0.5 + \#/7) + 10m (A), & t > 15 \text{ ms} \end{cases}$$

3. La carga eléctrica en un conductor se divide en tres partes y se comporta como el número de estudiantes en una universidad. Primero, decrece a razón de  $4k(1 + \#/5)$  por cada año. Luego, por cambios difíciles de explicar, se sabe que si bien el número en cinco años será el mismo de hoy, crecerá 50% dos años más adelante, cuando será  $50k(1 + \#/5)$ . Por último, y de ahí en adelante, el número es invariante.
  - a. Haga una gráfica para describir el número de estudiantes.
  - b. Calcule su ecuación.
  - c. Calcule y grafique el equivalente a la corriente,  $i(t)$ .

Nota por punto:

1. a. 1.0    2. a. 0.8    3. a. 0.5  
 b. 0.5    b. 0.8    b. 0.8  
 c. 0.6

Tiempo estimado:

1. 30 minutos, 2. 40 minutos, 3. 40 minutos

**Si utiliza Matlab, escriba todo el código en la hoja de solución.**

**Introduction to Electricity, Prof. Danilo Rairán, Nov/26/2020**

Name: \_\_\_\_\_ Code: \_\_\_\_\_

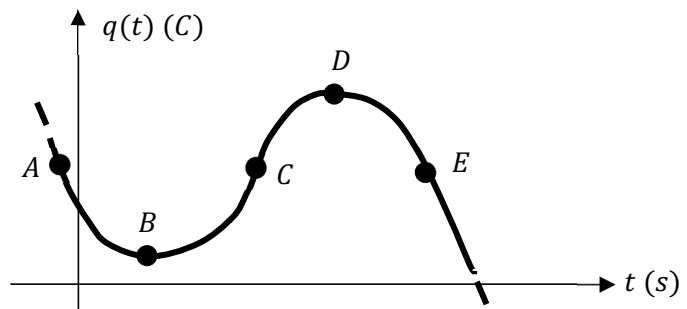
Group: \_\_\_\_\_ # = a number given by the professor during the test

1. Data points in the following table do not describe a parabola, but the best we can do in this moment is to define a parabola that sort of describe them. Compute the equation of a parabola that matches those points as better as possible.

$t$ (s)	0	$0,03e-5$	$0,06e-5$	$0,09e-5$	$0,12e-5$	$0,15e-5$	$0,18e-5$
$i$ (A)	0	$\# * 0,28e-8$	$\# * 0,46e-8$	$\# * 0,48e-8$	$\# * 0,34e-8$	$\# * 0,07e-8$	$-\# * 0,22e-8$

2. If  $A = (-2m, 8\mu)$ ,  $B = (1m, 6\mu - \#\mu/7)$ ,  
 $C = (4m, 8\mu)$ ,  $D = (6m, 10\mu + \#\mu/7)$ ,  
 $E = (8m, 8\mu)$

- a) compute an equation to describe  $q(t)$ ,  
 b) compute  $i(t)$ , c) plot  $i(t)$ .



3. Given the equation for  $i(t)$  answer the following questions: a)  $i(4m) = ?$ , b)  $t = ?$  if  $i = 11 mA$ , c)  $t = ?$  if  $i = 8 mA$ .

$$i(t) = \begin{cases} (-1.5 + \#/7)t - 5m(-1.5 + \#/7) + 10m (A), & t < 5 ms \\ -120t^2 + \frac{12}{5}t + 1m (A), & 5ms < t < 15ms \\ (0.5 + \#/7)t - 15m(0.5 + \#/7) + 10m (A), & t > 15 ms \end{cases}$$

4. The electric charge in one point of a circuit changes as the amount of honey in a beehive. The beehive is full at the end of fall, then decreases 20% during winter. Contrary with it is expected, it decreases during spring till 60% of the maximum, then at the end of summer it is 70%, when usually starts to grow linearly to be again 100% at the end of fall.

- a) Make a plot describing the amount of honey in the beehive. b) Compute the equation.

--

- |          |             |             |             |
|----------|-------------|-------------|-------------|
| 1. 1.0/5 | 2. a) 0.7/5 | 3. a) 0.4/5 | 4. a) 0.6/5 |
|          | b) 0.5/5    | b) 0.4/5    | b) 0.9/5    |
|          | c) 0.3/5    | c) 0.2/5    |             |

Introduction to Electricity, Prof. Danilo Rairán, Jan/27/2022, second test

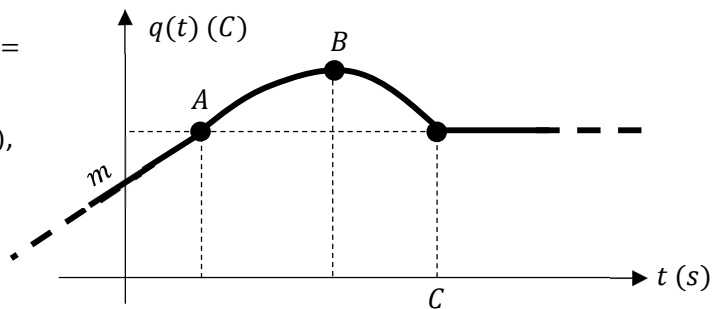
Name: \_\_\_\_\_ Code: \_\_\_\_\_

Group: \_\_\_\_\_ # = a number given by the professor during the test

1. The function  $i(t) = (t - \#)(t + \#)t$  (A) is not a parabola but given that the best knowledge we have so far to analyze it is a second order polynomial, then compute a parabola that approximates the function  $i(t)$  for  $t \geq 0$  s. Explain the procedure of approximation.

2. If  $m = \# \times 10^{-3}$ ,  $A = (\# \times 10^{-3}, \# \times 10^{-6})$ ,  $B = (2.5\# \times 10^{-3}, 2\# \times 10^{-6})$ ,  $C = 4\# \times 10^{-3}$ ,

a) compute an equation to describe  $q(t)$ ,  
b) compute  $i(t)$ , c) plot  $i(t)$ .



3. Given the equation for  $i(t)$  answer the following questions: a)  $i(0.5\#m) = ?$ , b)  $t = ?$  if  $i = 1.5\# \mu A$ , c)  $t = ?$  if  $i = 0.5\# \mu A$ .

$$i(t) = \begin{cases} (t - \#m)^2 + 2\#\mu & (A) , t < \# ms \\ -1mt + 3\#\mu & (A) , \# ms < t < 2\# ms \\ (t - 2\#m)^2 + \#\mu & (A) , t > 2\# ms \end{cases}$$

4. The number of transistors in a computer change similarly to the electric current in a circuit. It was  $25 + 10\#$  millions in 2016, it grew to  $50 + 10\#$  millions in 2018 and reached an outstanding value of  $100 + 10\#$  millions in 2020. However, it was not possible to continue that tendency of growing, instead, the number of transistors in a computer has been constantly increasing  $20 + 10\#$  million transistors per year.

a) Make a plot describing the number of transistors in a computer. b) Compute the equation, use scientific notation.

--

1. 1.0/5

2. a) 0.7/5

3. a) 0.4/5

4. a) 0.6/5

b) 0.5/5

b) 0.4/5

b) 0.9/5

c) 0.3/5

c) 0.2/5